

1. **Propositional Logic:** Given the interpretation $W = \{a, b, c\}$. For each of the following formulas, determine if W is a model for it:

$$(a \wedge b) \tag{1}$$

$$(b \rightarrow d) \tag{2}$$

$$b \wedge ((c \rightarrow e) \rightarrow d) \tag{3}$$

$$e \vee (c \wedge \neg d) \tag{4}$$

$$\neg d \rightarrow \neg e \tag{5}$$

2. **Propositional Logic:** Define an interpretation W which is a model for *all* of the following formulas:

$$(a \wedge \neg b) \tag{6}$$

$$(b \rightarrow c) \tag{7}$$

$$(c \vee d \vee \neg a) \tag{8}$$

$$(a \rightarrow e) \tag{9}$$

$$(e \rightarrow (\neg a \vee \neg b \vee \neg c \vee \neg d)) \tag{10}$$

3. **Predicate Logic:** Given the interpretation

$$W = \{Lannister(Tywin), Lannister(Tyrion), \\ Lannister(Cersei), Lannister(Jaime), \\ owes(Tyrion, Bronn), owes(Jaime, Brienne), \\ owes(Brienne, Catelyn), \\ paidDebt(Tyrion, Bronn), \\ paidDebt(Jaime, Brienne)\}$$

over the Domain $D = \{Tywin, Tyrion, Cersei, Jaime, Bronn, Brienne, Catelyn\}$. For each of the following formulas, determine if W is a model for it:

$$\forall x \forall y \in Lannister : owes(y, x) \rightarrow paidDebt(y, x) \tag{11}$$

$$\exists x \forall y : \neg owes(x, y) \tag{12}$$

$$\exists x \forall y : \neg owes(y, x) \tag{13}$$

$$\forall y \exists x : \neg owes(y, x) \tag{14}$$

$$\forall x : owes(x, Catelyn) \rightarrow \neg Lannister(x) \tag{15}$$

4. **Predicate Logic:** Define an interpretation W which is a model for *none* of the following formulas.

$$\forall x : \text{bird}(x) \tag{16}$$

$$\forall x \exists y : \text{eats}(x, y) \tag{17}$$

$$\neg \exists x : \text{cat}(x) \tag{18}$$

$$\forall x : \text{cat}(x) \rightarrow \neg \exists y \text{eats}(y, x) \tag{19}$$

$$\neg \text{dog}(\text{pluto}) \tag{20}$$

5. **Transition Systems:** Below you are given the state s_0 and the effects e_1, e_2, e_3 of three actions. Apply e_1 to s_0 and determine the resulting state s_1 . Apply e_2 to s_1 and determine the resulting state s_2 . Finally, apply e_3 to s_2 and determine a final state s_3 .

$$s_0 = \{ \text{at}(\text{Sherlock}, \text{BakerStreet}), \text{murderer}(\text{Moriarty}), \text{victim}(\text{ReginaldMusgrave}) \}$$

$$e_1 = (\forall x : \text{when}(\text{at}(\text{Sherlock}, x)) (\neg \text{at}(\text{Sherlock}, x))) \wedge \text{at}(\text{Sherlock}, \text{ScotlandYard})$$

$$e_2 = (\forall x : \text{when}(\text{victim}(x)) (\text{knowsVictim}(\text{Sherlock}, x))) \wedge$$

$$(\forall x : \text{when}(\text{murderer}(x)) \text{knowsMurderer}(\text{Sherlock}, x))$$

$$e_3 = \text{when}(\exists x : \text{murderer}(x) \wedge \text{knowsMurderer}(\text{Sherlock}, x)) (\text{solvedCrime}(\text{Sherlock}))$$

6*. **Bonus Points** Show that the negation of an effect formula (as defined on slide 51 in lecture 1) is not necessarily an effect formula.